

Q1].. Suppose that the parametric curve $x = f(t)$, $y = g(t)$ is such that $g'(1) = 0$. Is it true that the curve **must** have a horizontal tangent line at the point $(f(1), g(1))$? Explain your answer.

$$\frac{dy}{dx} \Big|_{t=1} = \frac{\frac{dy}{dt} \Big|_{t=1}}{\frac{dx}{dt} \Big|_{t=1}} \quad \dots \text{really} \quad \lim_{t \rightarrow 1} \frac{g'(t)}{f'(t)}$$

If $f'(1) \neq 0$ then $\frac{g'(1)}{f'(1)} = 0$ & we have horizontal ~~slp~~ tangent.

If $f'(1) = 0$, then we need to compute limit

$$\begin{aligned} \text{eg } g'(t) &= t^2 - 1 & \Rightarrow & \lim_{t \rightarrow 1} \frac{g'(t)}{f'(t)} = \lim_{t \rightarrow 1} \frac{t^2 - 1}{t - 1} \\ f'(t) &= t - 1 & & = \lim_{t \rightarrow 1} (t + 1) = 2 \end{aligned}$$

$$g(t) = \frac{t^3}{3} - t + 7$$

$$f(t) = \frac{t^2}{2} - t + 4$$

Parametric curve
with tangent slope 2
at the point
 $(f(1), g(1))$.