

$$\underline{\underline{Q11}} \quad \frac{d}{dx} \left(\int_x^\pi \sqrt{1+\sec t} dt \right) = \frac{d}{dx} \left(- \int_\pi^x \sqrt{1+\sec t} dt \right)$$

$$\text{Fund. Thm} \rightarrow = - \sqrt{1+\sec(x)}$$

Q16

$$\frac{d}{dx} \left(\int_0^{x^4} \cos^2(\theta) d\theta \right) = \frac{d}{du} \left(\int_0^u \cos^2(\theta) d\theta \right) \cdot \frac{du}{dx}$$

$u = x^4$ Ch. Rule

$$\text{Fund. Thm} \rightarrow = \cos^2(u) \frac{du}{dx}$$

$$= \cos^2(x^4) \cdot 4x^3$$

$$= 4x^3 \cos^2(x^4)$$

Q20

$$\int_{-1}^1 x^{100} dx = \left[\frac{x^{101}}{101} \right]_{-1}^1 = \frac{1}{101} - \frac{(-1)}{101}$$

$$= \boxed{\frac{2}{101}}$$

Q26

$$\int_{-5}^5 \pi dx = \left[\pi x \right]_{-5}^5 = 5\pi - (-5\pi)$$

$$= \boxed{10\pi}$$

Q61

$$\lim_{n \rightarrow \infty} \sum_{i=1}^n \frac{i^3}{n^4} = \lim_{n \rightarrow \infty} \sum_{i=1}^n \left(\frac{i}{n} \right)^3 \cdot \frac{1}{n} = \int_0^1 x^3 dx = \left[\frac{x^4}{4} \right]_0^1 = \boxed{\frac{1}{4}}$$