Conceptual Problems

Please provide a short explanation for your answers in this section.

1. (3 points) True or False? The function f(x) = |x| + 1 has an inverse.

2. (3 points) True or False? If z_1 and z_2 are complex numbers, then $\overline{z_1 + z_2} = \overline{z_1} + \overline{z_2}$, where \overline{z} denotes the complex conjugate of the complex number z.

Computational Problems

Please show your work.

3. (4 points) The function given by $f(x) = k(2 - x - x^3)$ has an inverse function, and $f^{-1}(3) = 2$. Find the value of k. 4. (4 points) Write the product/quotient of the complex numbers in the form a + bi where a, b are real numbers.

a. (1+i)(3-2i)

b. $\frac{3+i}{3-i}$

5. (4 points) Find the (possibly complex) roots of the polynomial $f(x) = -2x^2 + 3x - 2$.

6. (4 points) Find the solution sets of the following.

a. 3|4x+1| - 7 = 11

b. $|4x + 1| \ge 21$

c. $|2x - 1| \le -1$.

7. (4 points) Write the standard form of the equation of the parabola with vertex (-2, -2) and passes through (-1, 0).

9. (4 points) Find an absolute value inequality with solution set [-5, 3].

10. (4 points) Sketch the graph of the quadratic function $f(x) = -x^2 - 2x + 1$. Identify the vertex, axis of symmetry, and x-intercepts.