

2.5.4 Let R_i , B_i , and W_i be the events that red, black, and white chips are drawn from urn i , $i = 1, 2$. Then $P(\text{both chips drawn are same color}) = P((R_1 \cap R_2) \cup (B_1 \cap B_2) \cup (W_1 \cap W_2)) = P(R_1) \cdot P(R_2) + P(B_1) \cdot P(B_2) + P(W_1) \cdot P(W_2)$ [because the intersections are mutually exclusive and the individual draws are independent]. But $P(R_1) \cdot P(R_2) + P(B_1) \cdot P(B_2) + P(W_1) \cdot P(W_2) = \left(\frac{3}{10}\right)\left(\frac{2}{9}\right) + \left(\frac{2}{10}\right)\left(\frac{4}{9}\right) + \left(\frac{5}{10}\right)\left(\frac{3}{9}\right) = 0.32$.

2.5.14 $P(A) = \frac{3}{6}$, $P(B) = \frac{2}{6}$, $P(C) = \frac{6}{36}$, $P(A \cap B) = \frac{6}{36}$, $P(A \cap C) = \frac{3}{36}$, $P(B \cap C) = \frac{2}{36}$, and

$P(A \cap B \cap C) = \frac{1}{36}$. It follows that A , B , and C are mutually independent because

$$P(A \cap B \cap C) = \frac{1}{36} = P(A) \cdot P(B) \cdot P(C) = \frac{3}{6} \cdot \frac{2}{6} \cdot \frac{6}{36}, P(A \cap B) = \frac{6}{36} = P(A) \cdot P(B) = \frac{3}{6} \cdot \frac{2}{6},$$

$$P(A \cap C) = \frac{3}{36} = P(A) \cdot P(C) = \frac{3}{6} \cdot \frac{6}{36}, \text{ and } P(B \cap C) = \frac{2}{36} = P(B) \cdot P(C) = \frac{2}{6} \cdot \frac{6}{36}.$$

2.5.20 Let $A_H, A_T, B_H, B_T, C_H,$ and C_T denote the events that players $A, B,$ and C throw heads and tails on individual tosses. Then $P(A \text{ throws first head}) = P(A_H \cup (A_T \cap B_T \cap C_T \cap A_H) \cup \dots)$

$$= \frac{1}{2} + \frac{1}{2} \left(\frac{1}{8} \right) + \frac{1}{2} \left(\frac{1}{8} \right)^2 + \dots = \frac{1}{2} \left(\frac{1}{1 - 1/8} \right) = \frac{4}{7}. \text{ Similarly, } P(B \text{ throws first head}) =$$

$$P((A_T \cap B_H) \cup (A_T \cap B_T \cap C_T \cap A_T \cap B_H) \cup \dots) = \frac{1}{4} + \frac{1}{4} \left(\frac{1}{8} \right) + \frac{1}{4} \left(\frac{1}{8} \right)^2 + \dots = \frac{1}{4} \left(\frac{1}{1 - 1/8} \right) = \frac{2}{7}.$$

$$P(C \text{ throws first head}) = 1 - \frac{4}{7} - \frac{2}{7} = \frac{1}{7}.$$