

## Permutations and Combinations

Let  $X$  be a finite set with  $|X|=n$ .

- ① A  $k$ -permutation of  $X$  is an ordered list of  $k$  distinct elements of  $X$ .
- ② A  $k$ -combination of  $X$  is an unordered list of  $k$  distinct elements of  $X$ .
- ③ A  $k$ -permutation with repetition of  $X$  is an ordered list of  $k$  elements of  $X$ .  
↑↑
- ④ A  $k$ -combination with repetition of  $X$  is an unordered list of  $k$  elements of  $X$ .

- ① number of  $k$ -permutations of  $X = P(n, k) = \frac{n!}{(n-k)!}$  ←
- ② number of  $k$ -combinations of  $X = C(n, k) = \frac{n!}{k!(n-k)!} = \binom{n}{k}$
- ③ number of  $k$ -permutations of  $X$  with repetition =  $n^k$  ←  
←
- ④ number of  $k$ -combinations of  $X$  with repetition =  $\binom{n+k-1}{n-1}$   
=  $\frac{(n+k-1)!}{(n-1)! k!}$