

Instructions: Give concise answers, but clearly indicate your reasoning.

**I.** Consider the solid in the first octant bounded by the three coordinate planes and the plane  $3x + 2y + z = 6$ .

- (6)
- (a) What are the  $x$  and  $y$ -intercepts of the plane?
  - (b) The base of the solid is a triangle in the  $xy$ -plane. In an  $xy$ -plane, draw a picture of the base, and give equations for its sides.
  - (c) Write a double integral to find the volume of the solid. Supply specific limits of integration, but *do not* carry out any further calculations or try to evaluate it.

**II.** A lamina occupies the unit square  $R$ , where  $0 \leq x \leq 1$  and  $0 \leq y \leq 1$ . Its density at  $(x, y)$  is proportional to  $x^3$ . Write definite integrals to calculate each of the following, but *do not* carry out the evaluation of the integrals.

- (a) The mass of the lamina.
- (b) The moment of the lamina with respect to the  $x$ -axis.
- (c) The  $x$ -coordinate of the center of mass of the lamina, where  $m$  is its mass.

**III.** Change the order of integration for the following integral, but *do not* carry out any further calculations or try to evaluate it:  $\int_0^8 \int_{\sqrt[3]{y}}^2 e^{x^4} dx dy$ .

**IV.** Using polar coordinates, evaluate the integral  $\iint_D 2e^{-x^2-y^2} dA$ , where  $D$  is the region bounded by  $y = \sqrt{4-x^2}$  and the  $x$ -axis.