

Quiz 5

Name: Key Row: _____

[7]

1. Use L'Hopital's rule to find $\lim_{x \rightarrow 0} \frac{\ln(\cos x)}{x^2}$.

$$\left(\frac{\ln(\cos 0)}{0^2} = \frac{\ln(1)}{0} = \frac{0}{0} \right)$$

$$= \lim_{x \rightarrow 0} \frac{\frac{1}{\cos x} \cdot (-\sin x)}{2x}$$

$$= \lim_{x \rightarrow 0} \frac{-\tan x}{2x} \quad \left(\frac{-\tan 0}{2 \cdot 0} = \frac{0}{0} \right)$$

$$= \lim_{x \rightarrow 0} \frac{-\sec^2 x}{2} = \lim_{x \rightarrow 0} \frac{-1}{2 \cos^2 x} = \frac{-1}{2(\cos 0)^2} = \boxed{\frac{-1}{2}}$$

3. Evaluate the integral, showing all work:

[6] a. $\int \frac{1/x}{\sqrt{1-(\ln x)^2}} dx = \int \frac{1}{\sqrt{1-u^2}} du = \arcsin u + C$

① $u = \ln x$
 ① $du = \frac{1}{x} dx$

② $= \arcsin(\ln x) + C$
 ①

[7]

b. $\int x \sin(3x) dx = uv - \int v du = x \left(\frac{-\cos(3x)}{3} \right) - \int \left(\frac{-\cos 3x}{3} \right) dx$

① $u = x$ $dv = \sin(3x) dx$
 $du = dx$ $v = \int \sin(3x) dx$
 ① $v = \frac{-\cos(3x)}{3}$

$= \frac{-x \cos(3x)}{3} + \frac{1}{3} \int \cos(3x) dx$
 $= \frac{-x \cos(3x)}{3} + \frac{1}{3} \frac{\sin(3x)}{3} + C$

$= \boxed{\frac{-x \cos(3x)}{3} + \frac{\sin(3x)}{9} + C}$