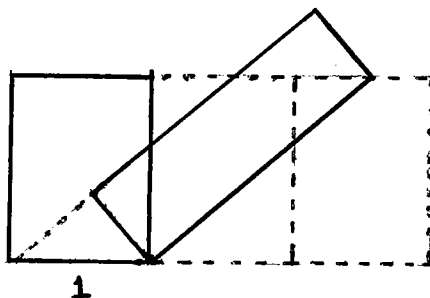


**Math 4513**  
**Assignment 3**

12. A polygon  $P$  is *convex* if the line segment connecting any two points of  $P$  is contained in  $P$ . Show that a convex polygon with  $n$  sides can be cut into  $n$  triangles.
13. *a.* Show that any polygon can be cut into convex pieces by extending the lines that form its edges.  
*b.* Deduce that any polygon can be cut into a finite number of triangles.
14. Show that given any triangle, you can cut it into a finite number of pieces and reassemble the pieces to form a rectangle.
15. Show that any rectangle may be cut into a finite number of pieces and the pieces reassembled to form a rectangle with width 1. (Hint: see the figure below.)



- 16.*a.* Show that any polygon can be cut into a finite number of pieces and the pieces reassembled to form a rectangle with width 1. (Use problems 13, 14, and 15.)  
*b.* Show that if  $P$  and  $P'$  are any two polygons of equal area, then  $P$  can be cut into a finite number of pieces and the pieces reassembled to form  $P'$ . (Use part a.)