

5.2 #8

10/10

$P(n)$ be statement we can form $5n$ dollars.

answer { 5, 8, 10, 13, 15, 16, 18, 20, 21, 23, 24, 25, 26, and all #s 28 and up }

We will prove this by showing $P(5), P(8), P(10), P(13), P(15), P(16), P(18), P(20), P(21), P(23), P(24), P(25), P(26), P(28), P(29), P(30), P(31)$ and $P(32)$

~~and we will show that if $P(k)$ is true for the $P(k+1)$ is true~~

Proof of $P(5) \dots P(28)$

Write instead: " $P(5)$ is true because $5 \cdot 5 = 25$ ", etc.

$P(5) = 5 \cdot 5 = 25$

$P(8) = 5 \cdot 8 = 40$

$P(10) = 5 \cdot 10 = 25 + 25$

$P(13) = 5 \cdot 13 = 40 + 25$

$P(15) = 5 \cdot 15 = 25 + 25 + 25$

$P(16) = 5 \cdot 16 = 40 + 40$

$P(18) = 5 \cdot 18 = 40 + 25 + 25$

$P(20) = 5 \cdot 20 = 25 + 25 + 25 + 25$

$P(21) = 5 \cdot 21 = 40 + 40 + 25$

$P(23) = 5 \cdot 23 = 40 + 25 + 25 + 25$

$P(24) = 5 \cdot 24 = 40 + 40 + 40$

$P(25) = 5 \cdot 25 = 25 + 25 + 25 + 25 + 25$

$P(26) = 5 \cdot 26 = 40 + 40 + 25 + 25$

$P(28) = 5 \cdot 28 = 40 + 25 + 25 + 25 + 25$

$P(29) = 5 \cdot 29 = 40 + 40 + 40 + 25$

$P(30) = 5 \cdot 30 = 25 + 25 + 25 + 25 + 25 + 25$

$P(31) = 5 \cdot 31 = 40 + 40 + 25 + 25 + 25$

$P(32) = 5 \cdot 32 = 40 + 40 + 40 + 40$

Very good.

~~Now we assume the inductive hypothesis, that $P(k)$ is true for all k with $28 \leq k \leq$~~

Now we assume the inductive hypothesis, that $P(n)$ is true for $28 \leq n \leq k$ where $k \geq 32$.

We want to show $P(k+1)$ is true. Because $k-4 \geq 28$, we know that $P(k-4)$ is true, that we can form $5(k-4)$ dollars. Adding one more 25-dollar certificate gives $5(k+1)$ dollars, which is what we set out to prove. This completes the proof by strong induction.

✓ Q.E.D.