Name:_

Math 166 Section 19061

October 6, 2011

Follow the instructions for each question and show enough of your work so that I can follow your thought process. If I can't read your work or answer, you will receive little or no credit!

For problems 1 - 6, evaluate the integrals.

$$1. \quad \int \frac{1}{x^2 + 3x - 4} \, dx$$

$$2. \quad \int \frac{x^3 - 4x - 10}{x^2 - x - 6} \ dx$$

3.
$$\int \frac{x^2 + 8x - 3}{x^3 + 3x^2} dx$$

$$4. \quad \int \frac{e^{3x}}{1+e^{2x}} \, dx$$

5.
$$\int x \sin^2 x \cos x \, dx$$

$$6. \quad \int \frac{dx}{1+e^x}$$

For problems 7 - 9, determine if the following integrals converge or diverge.

$$7. \quad \int_1^\infty \frac{\tan^{-1} x}{x^2} \, dx$$

$$8. \quad \int_0^2 \frac{\ln x}{\sqrt{x}} \, dx$$

$$9. \quad \int_0^1 \frac{dx}{\sqrt{1-x^2}}$$

For problems 10 - 12, find the length of the given curves.

10.
$$y = \ln(\cos x)$$
 on $0 \le x \le \frac{\pi}{4}$

11.
$$y = \frac{1}{6}(x^2 + 4)^{3/2}$$
, on $0 \le x \le 3$

12.
$$y = 2(x+4)^{3/2}$$
, on $0 \le x \le 2$

For problems 13 - 16, find the area of the surface obtained by rotating the given curve about the indicated axis.

13. $y = 1 - x^2$, on $0 \le x \le 1$ about the *y*-axis

14. $x = y^3$, on $1 \le y \le 2$ about the y-axis

15.
$$y = \frac{x^3}{6} + \frac{1}{2x}$$
, on $\frac{1}{2} \le x \le 1$ about the *x*-axis

16. Find the centroid of the region bounded by the curves $y = \sin x$, y = 0, x = 0, and $x = \pi$.

17. Find the centroid of the region bounded by y = x and $y = \sqrt{x}$.

18. Let $x = e^t$ and $y = t^2 + \sin t$. Compute $\frac{dy}{dx}$.

19. Set up the integral that represents the length of the curve given by $x = e^t + e^{-t}$ and $y = \ln(1+t^2)$ on $1 \le t \le 3$.

For problems 20 and 21, find a polar equation for the given curve represented by the Cartesian equation. 20. $x^2 - y^2 = 3xy$

21.
$$e^{x^2+y^2} = \frac{x}{y}$$

22. Find the values of θ on $0 \le \theta \le 2\pi$ of the curve $r = \cos \theta$ for which the tangent line is horizontal.

23. Define a curve by the following

$$x = \int_{1}^{t} \frac{\cos u}{u} du$$
 and $y = \int_{1}^{t} \frac{\sin u}{u} du$.

Find the length of the curve on $1 \le t \le e$.

24. Define a curve by the following

$$x = \int_0^t \cos\left(\frac{\pi u^2}{2}\right) du$$
 and $y = \int_0^t \sin\left(\frac{\pi u^2}{2}\right) du$.

Find the length of the curve on $1 \le t$. (Note the upper limit will be infinity.)