

MATH 4103

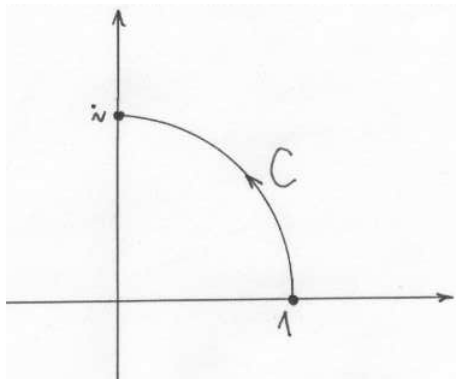
Quiz 8

Spring 2016

Name: \_\_\_\_\_

**Problem.** [1+1+1 points]

Let the contour  $C$  in  $\mathbb{C}$  be given by the equation  $z = Z(t) = e^{it}$ , where  $t$  varies from 0 to  $\frac{\pi}{2}$ . Let  $f(z) = z^2$ .



(a) Show that  $f(z)$  is analytic (just tell me what its derivative is), and use this fact to find  $\int_C f(z) dz$ .

(b) Find  $f(Z(t))$  and  $Z'(t)$ .

(c) Use your result from part (b) to compute  $\int_C f(z) dz$  directly from the definition of a contour integral.